

УПРАВЛЕНИЕ ЭФФЕКТИВНОСТЬЮ АВТОМАТИЗИРОВАННОГО КАДАСТРОВОГО ОФИСА

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Рассмотрена проблема управления эффективностью автоматизированного кадастрового офиса. Определены и проанализированы механизмы управления эффективностью, обоснована возможность управления эффективностью управляющим элементом отдельного кадастрового офиса. Определены направления повышения эффективности автоматизированной кадастровой системы.

Ключевые слова: управление, эффективность, кадастр, автоматизированная система.

PERFORMANCE MANAGEMENT AUTOMATED CADASTRAL OFFICE

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The problem of management efficiency of automated cadastral office. Identified and analyzed the mechanisms of performance management, the possibility of a performance management managing element separate cadastral office. The directions of increase of efficiency of an automated cadastre system.

Keywords: management, efficiency, cadastr, automated system.

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*Simon Kuznets Kharkiv National University of Economics, Kharkiv***ENHANCED MAC ALGORITHM BASED ON THE USE OF MODULAR TRANSFORMATIONS**

The article considers the choice of cycle functions in the provable persistent key universal hashing scheme, proposed model and method of forming codes of integrity and authenticity of data on the basis of modular transformations, computational complexity reduce algorithm of the hashing schemes implementation using cyclic functions. The object of the research is the process of improving the integrity and authenticity of data packets in security protocols of telecommunication networks. The developed enhanced method of forming a cascade MAC differs from the known (algorithm UMAC) using modular hashing on the last stage of the MAC forming that provides high collision properties of strictly universal hashing and safety performance at the level of modern means of demonstrable strength protection.

Keywords: codes of integrity and authenticity of data, a modular transformation, universal classes of hash functions.

Introduction

Studies have shown that the use of modular transformations allows realizing of provably resistant information hashing that satisfies the collisional properties of universal hash functions. Demonstrably safe level of strength is justified by reducing the problem of finding the source and / or the problem of recovering the secret key data to the solution of one of the well-known complexity-theoretic problems [1–3, 6].

At the same time, as shown by studies [1–3, 6], the universal hashing using modular transformations has a significant drawback - high computational complexity of the formation of the hash codes. In fact, for each information unit must perform a modular exponentiation that under transformation module appropriate orders significantly increases the time hashing information sequence. A promising direction in this regard is the development of multilayer universal hashing circuits using modular transformations on the last, the final stage of the hash code formation. This is as shown below, on the one hand provides a high collision properties of the resulting codes of integrity and authenticity of data generation circuit, on the other hand - provides high performance and provable strength level used transformations.

Problem statement

The use of multilayer hash key circuits allows building of effective mechanisms for monitoring the integrity and authenticity of information in telecommunication systems and networks. However, the known multilayer structure (for example, the algorithm UMAC) together with the high speed and the cryptographic strength when applying a cryptographic transformation layer (using symmetric block cipher) lose universal hash properties, which leads to deterioration of the properties of the collision properties of generated message authentication codes. The purpose of the study is to develop a method of forming codes of integrity and authenticity of data based on provably resistant hash key that allows providing high levels of security and with applying certain restrictions on the modular transformations provide high collisional properties.

Known methods

The analysis of [6–9] shows that the modular transformations are used today in the construction of keyless hash functions. Thus, in the fourth part of the international standard ISO/IEC 10118-4 defined two keyless hash function MASH-1 and MASH-2, which use modular arithmetic, namely the modular exponentiation to con-

struct hash [9]. The very name of functions MASH-1 and MASH-2 occurs from abbreviated Modular Arithmetic Secure Hash (secure hashing based on modular arithmetic), emphasizing the use of modular transformations in

the formation of the hash image. Table 1 shows the results of a comparative analysis of performance of some keyless hash functions, including the hash function on the modular arithmetic MASH-1 and MASH-2 [7].

Table 1

A comparative analysis of some keyless hash functions

The hash function	The length of hash	Applied conversion	Processing speed	Security model (by NESSIE)
SHA-2	256, 384, 512	logical and arithmetic	$10^8..10^9$ bit/sec	Practical Security
Whirlpool	512	In finite Galois fields	$10^7..10^8$ bit/sec	Practical Security
GOST 34311-95	256	Block symmetric encryption	$10^7..10^8$ bit/sec	Practical Security
RIPEMD-160	160	logical and arithmetic	$10^8..10^9$ bit/sec	Practical Security
MASH-1	*	Modular squaring	$10^5..10^6$ bit/sec	** "Provable" Security
MASH-2	*	Modular exponentiation $28+1 = 257$	$10^4..10^5$ bit/sec	** "Provable" Security

* Determined by the dimension of the conversion module

** If the parameters of the modular exponentiation comply with the limits for RSA-like systems

$$a \equiv (x^2) \pmod{n}$$

requires significantly fewer operations.

The analysis showed that the major drawback of hash functions MASH-1 and MASH-2 is the low hash code formation rate. In fact, it is determined by the speed of RSA-like encryption, which is 2-3 orders of magnitude slower than modern block symmetric ciphers. However, due to the presence of the possibility of using the existing modular arithmetic hardware and software used in asymmetrical RSA-like cryptosystems, as well as because of the possibility of providing a provable strength level (on the classification of security models NESSIE) considered keyless hash MASH-1 and MASH-2 were standardized [7, 9, 16].

It should be noted, however, that the use of a quadratic cycle function does not lead to construction of a universal hashing. Next to the computational complexity is a cyclic function

$$f(x_i, H_{i-1}) = (x_i \oplus H_{i-1})^e \pmod{N}, \quad (1)$$

inversion problem which is associated with the solution of the complexity-theoretic problem in RSA, where

$$\gcd(e, \phi(p, q)) = 1, \quad N = pq.$$

Thus, the use of cyclic function (1) based on modular exponentiation allows to construct a provably resistant universal hash function only under the constraints on the value of the modular exponent and absolute value of the change.

Another candidate for the cyclic function in the iterative hashing scheme is a function of the form:

$$f(x_i, H_{i-1}) = (\alpha^{x_i \oplus H_{i-1}}) \pmod{p}, \quad (2)$$

inversion problem which is associated with the solution of the complexity-theoretic problem of the discrete logarithm.

Use of a cyclic function ensures the construction of provably resistant hash, collision properties which satisfy the conditions of universality.

Thus, studies have shown that for the construction of universal hash information with provable security level should be used the cyclic function of the form (1) or of the form (2).

Development of algorithms for iterative key hashing with demonstrable strength based on modular transformations.

Iterative key hash algorithms with demonstrable strength based on the use of modular transformations is based algorithm MASH-1, subject to change initialization

Development of a universal key hashing method with demonstrable strength based on modular transformations

In the basis of the proposed universal key hashing method with provable strength is the use of modular transformations, providing reduction of the problem of finding the inverse image or a secret key in hashing scheme to one of the well-known complexity-theoretic problems. Such a justification of strength by security models classification NESSIE is considered to be provable security, thus emphasizing the reducibility cryptanalysis to one of the well-known computationally intractable in a given time complexity-theoretic problems [6].

Studies have shown that the most appropriate solution should obviously consider the use of the cyclic function, the problem of inverting which is associated with the solution of the complexity-theoretic problem of the extraction of square roots modulo n.

Under certain restrictions on the values of the composite module n this computational complexity inverting problem comparable to the problems of factorization and discrete logarithms. At the same time, the direct calculation of the values of

vectors and use of the above cyclic functions satisfying certain restrictions on used modular transformations.

Designed algorithms differ from the keyless hash algorithms MASH-1 and MASH-2 basically, by system settings and the determination of constants. In addition, the proposed schemes are key hashing, as the secret key data used interchangeable initialization vector $H_0 = \text{Key}$. For applied modular transformations in key hashing cyclic function imposed limitations discussed above.

Thus, the proposed universal hashing method using modular transformations allows formation of authenticators (hashes) to provide the required performance security. Designed algorithms allow practically implement the proposed hashing schemes in software and in hardware form.

Experiments

Development of proposals for the implementation of the iterative hash key with demonstrable strength using modular transformations.

The proposed universal hashing method is an iterative scheme of formation of the hash code with the cyclic function, built using modular transformations. To ensure high collision properties of universal hashing proposed cyclic function must be implemented with the use of the expressions (1) or (2) with the corresponding constraints on the modular transformations.

The analysis shows that the most expensive from a computational point of view the operation in the implementation of cycle functions (1) and (2) is the operation of modular exponentiation. With the direct exponentiation operations through the chain of multiplications, computational complexity of the implementation of such cyclic functions increases in proportion to the exponent, i.e. for the construction of x the power n generally needs $n - 1$ multiplications:

$$x^n = \underbrace{x \cdot x \cdot x \cdot \dots \cdot x}_{n-1 \text{ multiplications}}$$

An asymptotic estimate of the computational complexity of this exponentiation operation implementation is $O(n)$ multiplications.

To reduce the computational complexity of the implementation of the hashing scheme using cyclic functions (1) and (2) algorithm applied for fast exponentiation, which based on the representation of x^n in the following form:

$$x^n = x^{((\dots((m_k \cdot 2 + m_{k-1}) \cdot 2 + m_{k-2}) \cdot 2 + \dots + m_1) \cdot 2 + m_0)} = ((\dots(((x^{m_k})^2 \cdot x^{m_{k-1}})^2 \dots)^2 \cdot x^{m_1})^2 \cdot x^{m_0}), \tag{3}$$

where $(m_k, m_{k-1}, \dots, m_0)$ – binary representation of n , i.e. $m_i \in \{0,1\}$ and

$$n = m_k \cdot 2^k + m_{k-1} \cdot 2^{k-1} + \dots + m_1 \cdot 2 + m_0 \tag{4}$$

Rearranging the factors in the representation of x^n we obtain the following expression:

$$x^n = x^{m_0} \cdot (x^2)^{m_1} \cdot (x^2)^{m_2} \cdot (x^2)^{m_3} \cdot \dots \cdot (x^{2^k})^{m_k},$$

which implies that for the construction of a number x to the power of n required to implement at most k operations of squaring and at most k operations of multiplication, where $k + 1$ – number of elements in the binary number n , i.e. $k = (\log_2 n) - 1$. Thus, the computational complexity of calculating the asymptotic x^n can be estimated as $O(\log_2 n)$.

The above algorithm can significantly speed up the computation of cyclic functions (1) and (2) underlying the proposed method of universal hashing. Table 2 shows the dependence of the implementation complexity of the operation of exponentiation through a chain of multiplications and through the representation (3), (4), indicating the minimum necessary order of the conversion module to achieve the required level of security.

Table 2

Dependence of the implementation complexity regarding the exponentiation method

Exponentiation method	Procedure for conversion module / equivalent length of symmetric cryptographic algorithm key		
	1024 / 80	3072 / 128	15360 / 256
Through a series of multiplications	10308	10924	104623
Fast exponentiation algorithm	2046	6142	30718

The data in the second row of table 2 shown using the equivalence conditions (on computational complexity) of the squaring and multiplication operations.

The last row of table 2 is, in fact, is the computational complexity estimate of the proposed hashing scheme. Thus, at the lowest level of strength (cardinality of the set of key data block symmetric cipher is equal to 2^{80}) to calculate one value of cyclic function takes no more than 2046 operations multiplications. For a sufficient level of strength (cardinality of the set of key data BSC equal to 2128) relevant to the national standard

encryption USA FIPS-197 (AES), to calculate the cyclic function need to do no more than 6142 multiplications. For high-level strength (cardinality of the set of key data BSC equal to 2256), corresponding to the current domestic standard symmetric cryptoconversion GOST 28147-89, to calculate the cyclic function does not need to perform more than 30718 multiplications.

Developing a model of MAC cascade formation using modular transformations and justification of practical recommendations on its use. The article proposes a cascade formation model of codes of integrity and au-

thenticity of data (MAC) using the modular transformations.

The proposed model is based on a multi-layer universal hashing circuit using the last, the final stage of modular transformations.

Properties of multilayer (composite) design is best explained with the help of mappings language [4, 5]. Let X, Y, U are sets of n, m, u elements, $n < m < u$. H_1 is a set of functions f_1 performing the mapping $X \rightarrow U$ and H_2 is a set of functions f_2 performing the mapping $U \rightarrow Y$. Then $H = H_2 \circ H_1$ is a set of functions f , which is the composition $f = f_1 \circ f_2$.

Characteristics of a multilayered structure presented by the results of the following theorem [1–3].

Theorem 1. The composition of the universal hash functions class $\varepsilon_1 - U(N_1, n, u)$ and strictly universal hash functions class $\varepsilon_2 - SU(N_2, u, m)$ is strictly a universal class with parameters $\varepsilon - SU(N_1 N_2, n, m)$, where $\varepsilon = \varepsilon_1 + \varepsilon_2 - \varepsilon_1 \varepsilon_2$.

Thus, using the composition of authentication codes algorithms that are equivalent to an algorithm for computing the universal and strictly universal hash functions classes we obtain a multi-layer scheme for generating MAC [11-15]. Properties thus generated codes of integrity and authenticity of data will satisfy the properties of strictly universal class of hash functions.

In the method of forming codes of integrity and authenticity of data, the first layers are proposed to be realized with traditional UMAC high-speed but cryptographically weak universal hashing schemes algorithm, the last layer is proposed to implement using the developed safe (cryptographically strong) strictly universal hashing scheme based on the modular transformations. Formally, the proposed cascade formation scheme of codes of integrity and authenticity of data shown in Figure 1.

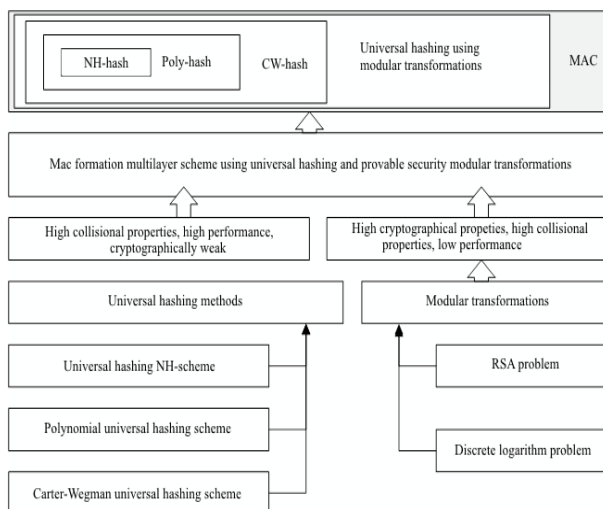


Fig. 1. Proposed cascade formation scheme control codes of integrity and authenticity of data using the modular transformations

The main part of the information data is processed first layers of universal hashing. Formed because of such conversion hash code on the last processed final stage cryptographically strong universal hash function based on the modular transformation.

Thus, based on the proposed scheme, MAC formation using modular transformations is used:

- on the first layers high-speed universal hashing methods (NH-hashing, polynomial hashing, Carter-Wegman hashing) are used;
- on the last layer secure strictly universal hashing based on modular transformations (using cyclic functions (1) and / or (2)) is use.

The work [3] proposes technique of statistical studies of collisional properties of MAC, in particular, introduces statistical indicators characterizing the collision properties of forming circuit of control codes integrity and authenticity of data, allowing using methods of probability theory and mathematical statistics to obtain estimates with prescribed confidence interval and the required accuracy. Experimental studies of collisional properties of message authentication codes UMAC for the relevant sections of the conversion:

- in the first stage investigate collision properties of a mini-version of the universal hashing. To do this, the theoretical estimates of the number of generated hash codes collisions occurring in the course of the experiment must be confirmed;
- in the second stage conduct an experimental study of the properties of pseudo-conflict substrates based on analysis of the properties of the reduced Baby-Rijndael cipher model. Similar studies in the available literature aren't described, appear to be carried out by us for the first time;

– in the third stage, conduct an experimental study of the properties of collision properties generated by using mini-UMAC integrity and authenticity of data control. This is the most important part of the research, as it would answer the question of maintaining the properties of universal hashing after application of the cryptographic transformation of the information layer.

Estimates of the number of collisions generated elements will be carried out focusing on the universal hashing collision properties. In fact, we need to confirm or refute the hypothesis of the saving of universal hashing collision properties at all stages of generating of the mini-UMAC control codes of integrity and authenticity of data.

Results

Consider a cyclic functions MASH-1 and MASH-2 for the construction of the key universal hash functions and hash option when the initial state (initialization vector) is given by some key rule, i.e. choose $H_0 = Key$. In this case, we have a certain class of hash functions, depending on the parameter Key. For experimental studies selected the following parameters: $p = 17$,

$q = 19$, $N = 323$. Study were to verify the conditions of universal hashing with exhaustive search of all the values of initialization vectors ($Key = 0, \dots, 2^m - 1$, $m = 8$) for a sample of the population values of information blocks. The results obtained are summarized in Table 3.

Table 3

The results of studies of collisional properties of a key hashing algorithms built on the basis of MASH-1 and MASH-2 by changing the values of the initialization vector secret key

	Based algorithm	
	MASH-1	MASH-2
$\tilde{m}(n_1)$	41,42	0
$\tilde{D}(n_1)$	42,74	0
$P_d = P(\tilde{m}(n_1) - m(n_1) < 5)$	0,98	≈ 1
$\tilde{m}(n_2)$	3,99	1
$\tilde{D}(n_2)$	0,01	0
$P_d = P(\tilde{m}(n_2) - m(n_2) < 0,025)$	0,99	≈ 1
$\tilde{m}(n_3)$	0,26	0,31
$\tilde{D}(n_3)$	0,21	0,22
$P_d = P(\tilde{m}(n_3) - m(n_3) < 0,1)$	0,97	0,97

Thus, studies have shown that the application of transformations using modular arithmetic allows to build universal and strictly universal hash functions classes, which on one hand allow high collision properties, on the

other hand, under certain restrictions on the value of the modular exponential ensure high security and the applicability of the model demonstrable strength.

Table 4 shows a comparison of the computational complexity of some hash functions. Data on performance for the proposed MAC scheme with modular transformations are given for the minimum level of persistence (cardinality of the set of key data block symmetric cipher is equal to 2^{80}) and a sufficient level of strength (for modular transformations equivalent length block symmetric cipher key is 128 bits). Length of the MAC generated is 80, and 128 bits, respectively.

For all the functions listed in Table 4 (except the proposed using modular transformations) specific complexity of the codes of integrity and authenticity of data is not dependent on the amount of data processed. For the proposed model using a modular transformations specific complexity with increase of length of data to be processed is reduced. So for a high level of strength (equivalent length block symmetric cipher key is 128 bits) already for data blocks of 32768 bytes is comparable to well-known and used in network security protocols, algorithms form the MAC. For the lowest level of strength (cardinality of the set of key data block symmetric cipher is equal to 2^{80}) the proposed scheme of codes of integrity and authenticity of data cascade formation using modular transformations already for data packets of 2048 bytes is not inferior in performance used to date the formation of the MAC algorithm in network security protocols, including protocols IPsec.

Table 4

Estimate of the complexity of different MAC forming schemes

Algorithm	The length of the input data, bytes					
	2048	4096	8192	16384	32768	65536
HMAC-MD5 (128 bits)	9	9	9	9	9	9
HMAC-RIPE-MD (160 bits)	27	27	27	27	27	27
HMAC-SHA-1 (160 bits)	25	25	25	25	25	25
HMAC-SHA-2 (512 bits)	84	84	84	84	84	84
CBC MAC-Rijndael (128 bits)	26	26	26	26	26	26
CBC MAC-DES (64 bits)	62	62	62	62	62	62
Proposed MAC scheme using modular transformations (80 bits)	38	22	14	10	8	7
Proposed MAC scheme using modular transformations (128 bits)	294	150	78	42	24	15

Conclusions

In this paper were obtained the theoretical generalization and new solution of scientific-applied problem, which is to develop and research of models and methods of effective mechanisms for monitoring the integrity and authenticity of data packets while minimizing the number of CPU cycles per byte of information to process to provide the necessary reliability and data security in telecommunications networks.

Scientific novelty of the work lies in the fact that:

1. For the first time to analyze the collision properties of the codes monitoring the integrity and authenticity an approach is suggested based on the creation of scale models (mini version) algorithms of UMAC, which allows them to retain the algebraic structure.

2. For the first time mathematical apparatus and methods for the analysis of statistical studies of collisional properties are suggested which allows to determine the distribution of codes formed on the entire set of key data and obtain estimates of collisional properties with the required accuracy.

3. For the first time model and method of forming codes of integrity and authenticity of data using at the final stage cryptographically strong strictly universal hash function based on modular transformations. The proposed solution provides high collision properties of strictly universal hashing, low computational complexity and high security performance at the level of modern means of cryptographic protection with provable security.

Practical advice on building a cascade formation schemes of MAC based on modular hashing was justified the implementation of which will ensure the delivery time information packet to 0.5 sec; safe time more than 200 years; the probability of imposing a false message is not more than 10⁻²⁵; the probability of message modification message is not more than 10⁻²⁵. The usage of the developed models and methods of forming the MAC to control the integrity and authenticity of data packets in security protocols of telecommunication networks and internal payment banking systems.

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МЕТОД КАСКАДНОГО ФОРМИРОВАНИЯ МАС С ИСПОЛЬЗОВАНИЕМ МОДУЛЯРНЫХ ПРЕОБРАЗОВАНИЙ

О.Г. Король

Обосновывается выбор цикловых функций в схеме доказуемо стойкого ключевого универсального хеширования, предлагается модель и метод формирования кодов контроля целостности и аутентичности данных на основе модулярных преобразований, алгоритм снижения вычислительной сложности реализации схем хеширования с использованием цикловых функций. Объектом исследования является процесс повышения целостности и аутентичности пакетов данных в протоколах безопасности телекоммуникационных сетей.

Ключевые слова: коды контроля целостности и аутентичности данных, модулярные преобразования, универсальные классы хеширующих функций.

МЕТОД КАСКАДНОГО ФОРМУВАННЯ МАС З ВИКОРИСТАННЯМ МОДУЛЯРНИХ ПЕРЕТВОРЕНЬ

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Обґрунтовується вибір циклових функцій у схемі доказово стійкого ключевого універсального гешування, пропонується модель і метод формування кодів контролю цілісності та автентичності даних на основі модулярних перетворень, алгоритм зниження обчислювальної складності реалізації схем хешування з використанням циклових функцій. Об'єктом дослідження є процес підвищення цілісності та автентичності пакетів даних в протоколах безпеки телекомунікаційних мереж.

Ключові слова: коди контролю цілісності та автентичності даних, модулярні перетворення, універсальні класи функцій гешування.